## NAG SMP Library

## Tuned and Enhanced Routines in the NAG SMP Library

The following sections list the user-callable routines that have been parallelised, or otherwise optimized.

Note: on some implementations, the equivalent vendor library routines may be substituted for some of the following list - consult the Users' Note for your implementation for further information.

## **1** Tuned Routines

C06FKF Circular convolution or correlation of two real vectors, extra workspace for greater speed Multiple one-dimensional real discrete Fourier transforms C06FPF Multiple one-dimensional Hermitian discrete Fourier transforms C06FQF C06FRF Multiple one-dimensional complex discrete Fourier transforms C06FUF Two-dimensional complex discrete Fourier transform Three-dimensional complex discrete Fourier transform C06FXF Discrete sine transform C06HAF C06HBF Discrete cosine transform C06HCF Discrete quarter-wave sine transform Discrete quarter-wave cosine transform C06HDF Single one-dimensional real and Hermitian complex discrete Fourier transform, using complex C06PAF data format for Hermitian sequences C06PFF One-dimensional complex discrete Fourier transform of multi-dimensional data (using complex data type) C06PJF Multi-dimensional complex discrete Fourier transform of multi-dimensional data (using complex data type) C06PKF Circular convolution or correlation of two complex vectors C06PPF Multiple one-dimensional real and Hermitian complex discrete Fourier transforms, using complex data format for Hermitian sequences Multiple one-dimensional real and Hermitian complex discrete Fourier transforms, using C06POF complex data format for Hermitian sequences Multiple one-dimensional complex discrete Fourier transforms using complex data format C06PRF C06PSF Multiple one-dimensional complex discrete Fourier transforms using complex data format and sequences stored as columns Two-dimensional complex discrete Fourier transform, complex data format C06PUF Three-dimensional complex discrete Fourier transform, complex data format C06PXF C06RAF Discrete sine transform (easy-to-use) C06RBF Discrete cosine transform (easy-to-use) C06RCF Discrete quarter-wave sine transform (easy-to-use) Discrete quarter-wave cosine transform (easy-to-use) C06RDF F04AFF Solution of real symmetric positive-definite simultaneous linear equations using iterative refinement (coefficient matrix already factorized by F03AEF) Solution of real symmetric positive-definite simultaneous linear equations (coefficient matrix F04AGF already factorized by F03AEF) F04AHF Solution of real simultaneous linear equations using iterative refinement (coefficient matrix already factorized by F03AFF) F04AJF Solution of real simultaneous linear equations (coefficient matrix already factorized by F03AFF) LU factorization of real m by n matrix F07ADF F07AEF Solution of real system of linear equations, multiple right-hand sides, matrix already factorized by F07ADF (DGETRF) Refined solution with error bounds of real system of linear equations, multiple right-hand sides F07AHF LU factorization of complex *m* by *n* matrix F07ARF F07ASF Solution of complex system of linear equations, multiple right-hand sides, matrix already factorized by F07ARF (ZGETRF) Refined solution with error bounds of complex system of linear equations, multiple right-hand F07AVF

sides

F07BDF F07BEF	LU factorization of real $m$ by $n$ band matrix Solution of real band system of linear equations, multiple right-hand sides, matrix already
F07BHF	factorized by F07BDF (DGBTRF) Refined solution with error bounds of real band system of linear equations, multiple right-hand
E07DDE	sides
F07BRF F07BSF	LU factorization of complex $m$ by $n$ band matrix Solution of complex band system of linear equations, multiple right-hand sides, matrix already
10/051	factorized by F07BRF (ZGBTRF)
F07BVF	Refined solution with error bounds of complex band system of linear equations, multiple right- hand sides
F07CHF	Refined solution with error bounds of real tridiagonal system of linear equations, multiple right-hand sides
F07CVF	Refined solution with error bounds of complex tridiagonal system of linear equations, multiple right-hand sides
F07FDF	Cholesky factorization of real symmetric positive-definite matrix
F07FEF	Solution of real symmetric positive-definite system of linear equations, multiple right-hand sides, matrix already factorized by F07FDF (DPOTRF)
F07FHF	Refined solution with error bounds of real symmetric positive-definite system of linear equations, multiple right-hand sides
F07FRF	Cholesky factorization of complex Hermitian positive-definite matrix
F07FSF	Solution of complex Hermitian positive-definite system of linear equations, multiple right-hand sides, matrix already factorized by F07FRF (ZPOTRF)
F07FVF	Refined solution with error bounds of complex Hermitian positive-definite system of linear equations, multiple right-hand sides
F07GEF	Solution of real symmetric positive-definite system of linear equations, multiple right-hand sides, matrix already factorized by F07GDF (DPPTRF), packed storage
F07GHF	Refined solution with error bounds of real symmetric positive-definite system of linear equations, multiple right-hand sides, packed storage
F07GSF	Solution of complex Hermitian positive-definite system of linear equations, multiple right-hand sides, matrix already factorized by F07GRF (ZPPTRF), packed storage
F07GVF	Refined solution with error bounds of complex Hermitian positive-definite system of linear equations, multiple right-hand sides, packed storage
F07HEF	Solution of real symmetric positive-definite band system of linear equations, multiple right- hand sides, matrix already factorized by F07HDF (DPBTRF)
F07HHF	Refined solution with error bounds of real symmetric positive-definite band system of linear equations, multiple right-hand sides
F07HSF	Solution of complex Hermitian positive-definite band system of linear equations, multiple right-hand sides, matrix already factorized by F07HRF (ZPBTRF)
F07HVF	Refined solution with error bounds of complex Hermitian positive-definite band system of linear equations, multiple right-hand sides
F07JHF	Refined solution with error bounds of real symmetric positive-definite tridiagonal system of linear equations, multiple right-hand sides
F07JVF	Refined solution with error bounds of complex Hermitian positive-definite tridiagonal system of linear equations, multiple right-hand sides
F07MHF	Refined solution with error bounds of real symmetric indefinite system of linear equations, multiple right-hand sides
F07MVF	Refined solution with error bounds of complex Hermitian indefinite system of linear equations, multiple right-hand sides
F07NVF	Refined solution with error bounds of complex symmetric system of linear equations, multiple right-hand sides
F07PHF	Refined solution with error bounds of real symmetric indefinite system of linear equations, multiple right-hand sides, packed storage
F07PVF	Refined solution with error bounds of complex Hermitian indefinite system of linear equations, multiple right-hand sides, packed storage
F07QVF	Refined solution with error bounds of complex symmetric system of linear equations, multiple right-hand sides, packed storage
F07THF	Error bounds for solution of real triangular system of linear equations, multiple right-hand sides

F07TVF	Error bounds for solution of complex triangular system of linear equations, multiple right-hand sides
F07UEF F07UHF	Solution of real triangular system of linear equations, multiple right-hand sides, packed storage Error bounds for solution of real triangular system of linear equations, multiple right-hand
F07USF	sides, packed storage Solution of complex triangular system of linear equations, multiple right-hand sides, packed
	storage
F07UVF	Error bounds for solution of complex triangular system of linear equations, multiple right-hand sides, packed storage
F07VEF	Solution of real band triangular system of linear equations, multiple right-hand sides
F07VHF	Error bounds for solution of real band triangular system of linear equations, multiple right-hand sides
F07VSF	Solution of complex band triangular system of linear equations, multiple right-hand sides
F07VVF	Error bounds for solution of complex band triangular system of linear equations, multiple right-hand sides
F08AEF	QR factorization of real general rectangular matrix
F08AFF	Form all or part of orthogonal $Q$ from $QR$ factorization determined by F08AEF (DGEQRF) or F08BEF (DGEQPF)
F08AGF	Apply orthogonal transformation determined by F08AEF (DGEQRF) or F08BEF (DGEQPF)
F08ASF F08ATF	QR factorization of complex general rectangular matrix Form all or part of unitary $Q$ from $QR$ factorization determined by F08ASF (ZGEQRF) or
FUOAIF	F08BSF (ZGEQPF)
F08AUF	Apply unitary transformation determined by F08ASF (ZGEQRF) or F08BSF (ZGEQPF)
F08FEF	Orthogonal reduction of real symmetric matrix to symmetric tridiagonal form
F08FFF	Generate orthogonal transformation matrix from reduction to tridiagonal form determined by F08FEF (DSYTRD)
F08FSF	Unitary reduction of complex Hermitian matrix to real symmetric tridiagonal form
F08FTF	Generate unitary transformation matrix from reduction to tridiagonal form determined by F08FSF (ZHETRD)
F08GFF	Generate orthogonal transformation matrix from reduction to tridiagonal form determined by F08GEF (DSPTRD)
F08GTF	Generate unitary transformation matrix from reduction to tridiagonal form determined by F08GSF (ZHPTRD)
F08HEF	Orthogonal reduction of real symmetric band matrix to symmetric tridiagonal form
F08HSF	Unitary reduction of complex Hermitian band matrix to real symmetric tridiagonal form
F08JEF	All eigenvalues and eigenvectors of real symmetric tridiagonal matrix, reduced from real symmetric matrix using implicit $QL$ or $QR$
F08JJF	Selected eigenvalues of real symmetric tridiagonal matrix by bisection
F08JKF	Selected eigenvectors of real symmetric tridiagonal matrix by inverse iteration, storing eigenvectors in real array
F08JSF	All eigenvalues and eigenvectors of real symmetric tridiagonal matrix, reduced from complex
F08JXF	Hermitian matrix, using implicit $QL$ or $QR$ Selected eigenvectors of real symmetric tridiagonal matrix by inverse iteration, storing
	eigenvectors in complex array
F08KEF	Orthogonal reduction of real general rectangular matrix to bidiagonal form
F08KSF	Unitary reduction of complex general rectangular matrix to bidiagonal form
F08MEF	SVD of real bidiagonal matrix reduced from real general matrix
F08MSF	SVD of real bidiagonal matrix reduced from complex general matrix
F08PEF	Eigenvalues and Schur factorization of real upper Hessenberg matrix reduced from real general matrix
F08PKF	Selected right and/or left eigenvectors of real upper Hessenberg matrix by inverse iteration
F08PSF	Eigenvalues and Schur factorization of complex upper Hessenberg matrix reduced from complex general matrix
F08PXF	Selected right and/or left eigenvectors of complex upper Hessenberg matrix by inverse iteration
F08TAF	Computes all the eigenvalues, and optionally, the eigenvectors of a real generalized symmetric- definite eigenproblem, packed storage
F08TBF	Computes selected eigenvalues, and optionally, the eigenvectors of a real generalized symmetric-definite eigenproblem, packed storage

- F08TCF Computes all the eigenvalues, and optionally, the eigenvectors of a real generalized symmetricdefinite eigenproblem, packed storage (divide-and-conquer)
- F08TNF Computes all the eigenvalues, and optionally, the eigenvectors of a complex generalized Hermitian-definite eigenproblem, packed storage
- F08TPF Computes selected eigenvalues, and optionally, the eigenvectors of a complex generalized Hermitian-definite eigenproblem, packed storage
- F08TQF Computes selected eigenvalues, and optionally, the eigenvectors of a complex generalized Hermitian-definite eigenproblem, packed storage (divide-and-conquer)
- F11BEF Real sparse nonsymmetric linear systems, preconditioned RGMRES, CGS, Bi-CGSTAB or TFQMR method
- F11BSF Complex sparse non-Hermitian linear systems, preconditioned RGMRES, CGS, Bi-CGSTAB or TFQMR method
- F11GEF Real sparse symmetric linear systems, preconditioned conjugate gradient or Lanczos
- F11GSF Complex sparse Hermitian linear systems, preconditioned conjugate gradient or Lanczos
- F11MEF LU factorization of real sparse matrix
- F11MFF Solution of real sparse simultaneous linear equations (coefficient matrix already factorized)
- F11MHF Refined solution with error bounds of real system of linear equations, multiple right-hand sides
- F11MKF Real sparse nonsymmetric matrix matrix multiply, compressed column storage
- F11XAF Real sparse nonsymmetric matrix vector multiply
- F11XEF Real sparse symmetric matrix vector multiply
- F11XNF Complex sparse non-Hermitian matrix vector multiply
- F11XSF Complex sparse Hermitian matrix vector multiply
- F12ABF Implements a reverse communication interface for the Implicitly Restarted Arnoldi iteration for computing selected eigenvalues and, optionally, eigenvectors of a real nonsymmetric sparse (standard or generalized) eigenproblem
- F12AGF Computes approximations to selected eigenvalues of a real nonsymmetric banded (standard or generalized) eigenproblem and, optionally, the corresponding approximate eigenvectors and/or an orthonormal basis for the associated approximate invariant subspace

## 2 Enhanced Routines

- C02AKF All zeros of real cubic equation
- C02ALF All zeros of real quartic equation
- C02AMF All zeros of complex cubic equation
- C02ANF All zeros of complex quartic equation
- D01PAF Multi-dimensional quadrature over an *n*-simplex
- D02AGF ODEs, boundary value problem, shooting and matching technique, allowing interior matching point, general parameters to be determined
- D02EJF ODEs, stiff IVP, BDF method, until function of solution is zero, intermediate output (simple driver)
- D02HAF ODEs, boundary value problem, shooting and matching, boundary values to be determined
- D02HBF ODEs, boundary value problem, shooting and matching, general parameters to be determined D02NBF Explicit ODEs, stiff IVP, full Jacobian (comprehensive)
- D02NCF Explicit ODEs, stiff IVP, banded Jacobian (comprehensive)
- D02NDF Explicit ODEs, stiff IVP, sparse Jacobian (comprehensive)
- D02NGF Implicit/algebraic ODEs, stiff IVP, full Jacobian (comprehensive)
- D02NHF Implicit/algebraic ODEs, stiff IVP, banded Jacobian (comprehensive)
- D02NJF Implicit/algebraic ODEs, stiff IVP, sparse Jacobian (comprehensive)
- D02NMF Explicit ODEs, stiff IVP (reverse communication, comprehensive)
- D02NNF Implicit/algebraic ODEs, stiff IVP (reverse communication, comprehensive)
- D02SAF ODEs, boundary value problem, shooting and matching technique, subject to extra algebraic equations, general parameters to be determined
- D02TKF ODEs, general nonlinear boundary value problem, collocation technique
- D03FAF Elliptic PDE, Helmholtz equation, three-dimensional Cartesian co-ordinates
- D03NCF Finite difference solution of the Black–Scholes equations
- D03PCF General system of parabolic PDEs, method of lines, finite differences, one space variable
- D03PDF General system of parabolic PDEs, method of lines, Chebyshev  $C^0$  collocation, one space variable

D03PEF	General system of first-order PDEs, method of lines, Keller box discretisation, one space variable
D03PFF	General system of convection-diffusion PDEs with source terms in conservative form, method of lines, upwind scheme using numerical flux function based on Riemann solver, one space variable
D03PHF	General system of parabolic PDEs, coupled DAEs, method of lines, finite differences, one space variable
D03PJF	General system of parabolic PDEs, coupled DAEs, method of lines, Chebyshev $C^0$ collocation, one space variable
D03PKF	General system of first-order PDEs, coupled DAEs, method of lines, Keller box discretisation, one space variable
D03PLF	General system of convection-diffusion PDEs with source terms in conservative form, coupled DAEs, method of lines, upwind scheme using numerical flux function based on Riemann solver, one space variable
D03PPF	General system of parabolic PDEs, coupled DAEs, method of lines, finite differences, remeshing, one space variable
D03PRF	General system of first-order PDEs, coupled DAEs, method of lines, Keller box discretisation, remeshing, one space variable
D03PSF	General system of convection-diffusion PDEs with source terms in conservative form, coupled DAEs, method of lines, upwind scheme using numerical flux function based on Riemann solver, remeshing, one space variable
D05AAF	Linear non-singular Fredholm integral equation, second kind, split kernel
D05ABF	Linear non-singular Fredholm integral equation, second kind, smooth kernel
E02RAF	Padé approximants
E04FCF	Unconstrained minimum of a sum of squares, combined Gauss–Newton and modified Newton algorithm using function values only (comprehensive)
E04FYF	Unconstrained minimum of a sum of squares, combined Gauss–Newton and modified Newton algorithm using function values only (easy-to-use)
E04GBF	Unconstrained minimum of a sum of squares, combined Gauss–Newton and quasi-Newton algorithm using first derivatives (comprehensive)
E04GDF	Unconstrained minimum of a sum of squares, combined Gauss-Newton and modified Newton algorithm using first derivatives (comprehensive)
E04GYF	Unconstrained minimum of a sum of squares, combined Gauss–Newton and quasi-Newton algorithm, using first derivatives (easy-to-use)
E04GZF	Unconstrained minimum of a sum of squares, combined Gauss–Newton and modified Newton algorithm using first derivatives (easy-to-use)
E04HEF	Unconstrained minimum of a sum of squares, combined Gauss-Newton and modified Newton algorithm, using second derivatives (comprehensive)
E04HYF	Unconstrained minimum of a sum of squares, combined Gauss-Newton and modified Newton algorithm, using second derivatives (easy-to-use)
E04NCF	Convex QP problem or linearly-constrained linear least-squares problem (dense)
E04UFF	Minimum, function of several variables, sequential QP method, nonlinear constraints, using function values and optionally first derivatives (reverse communication, comprehensive)
E04USF	Minimum of a sum of squares, nonlinear constraints, sequential QP method, using function values and optionally first derivatives (comprehensive)
E04YCF	Covariance matrix for nonlinear least-squares problem (unconstrained)
F01ABF	Inverse of real symmetric positive-definite matrix using iterative refinement
F01ADF	Inverse of real symmetric positive-definite matrix
F02ECF	Selected eigenvalues and eigenvectors of real nonsymmetric matrix (Black Box)
F02FJF	Selected eigenvalues and eigenvectors of sparse symmetric eigenproblem (Black Box)
F02GCF	Selected eigenvalues and eigenvectors of complex nonsymmetric matrix (Black Box)
F02WDF	QR factorization, possibly followed by SVD
F02WUF	SVD of real upper triangular matrix (Black Box)
F02XUF	SVD of complex upper triangular matrix (Black Box)
F03AAF	Determinant of real matrix (Black Box)
F03ABF	Determinant of real symmetric positive-definite matrix (Black Box)
F03ADF	Determinant of complex matrix (Black Box)
F03AEF	$LL^{T}$ factorization and determinant of real symmetric positive-definite matrix

F03AFF F04ABF	LU factorization and determinant of real matrix Solution of real symmetric positive-definite simultaneous linear equations with multiple right-
F04AEF	hand sides using iterative refinement (Black Box) Solution of real simultaneous linear equations with multiple right-hand sides using iterative
F04ASF	refinement (Black Box) Solution of real symmetric positive-definite simultaneous linear equations, one right-hand side using iterative refinement (Black Box)
F04ATF	Solution of real simultaneous linear equations, one right-hand side using iterative refinement (Black Box)
F04BAF	Computes the solution and error-bound to a real system of linear equations
F04BBF	Computes the solution and error-bound to a real banded system of linear equations
F04BDF	Computes the solution and error-bound to a real symmetric positive-definite system of linear equations
F04BEF	Computes the solution and error-bound to a real symmetric positive-definite system of linear equations, packed storage
F04BFF	Computes the solution and error-bound to a real symmetric positive-definite banded system of linear equations
F04CAF	Computes the solution and error-bound to a complex system of linear equations
F04CBF	Computes the solution and error-bound to a complex banded system of linear equations
F04CDF	Computes the solution and error-bound to a complex Hermitian positive-definite system of linear equations
F04CEF	Computes the solution and error-bound to a complex Hermitian positive-definite system of linear equations, packed storage
F04CFF	Computes the solution and error-bound to a complex Hermitian positive-definite banded system of linear equations
F04JGF	Least-squares (if rank $= n$ ) or minimal least-squares (if rank $< n$ ) solution of $m$ real equations in $n$ unknowns, rank $\leq n, m \geq n$
F07AAF	Computes the solution to a real system of linear equations
F07ABF	Uses the $LU$ factorization to compute the solution, error-bound and condition estimate for a real system of linear equations
F07ANF	Computes the solution to a complex system of linear equations
F07APF	Uses the $LU$ factorization to compute the solution, error-bound and condition estimate for a complex system of linear equations
F07BAF	Computes the solution to a real banded system of linear equations
F07BBF	Uses the $LU$ factorization to compute the solution, error-bound and condition estimate for a real banded system of linear equations
F07BNF	Computes the solution to a complex banded system of linear equations
F07BPF	Uses the $LU$ factorization to compute the solution, error-bound and condition estimate for a complex banded system of linear equations
F07CBF	Uses the $LU$ factorization to compute the solution, error-bound and condition estimate for a real tridiagonal system of linear equations
F07CPF	Uses the $LU$ factorization to compute the solution, error-bound and condition estimate for a complex tridiagonal system of linear equations
F07FAF	Computes the solution to a real symmetric positive-definite system of linear equations
F07FBF	Uses the Cholesky factorization to compute the solution, error-bound and condition estimate for a real symmetric positive-definite system of linear equations
F07FNF	Computes the solution to a complex Hermitian positive-definite system of linear equations
F07FPF	Uses the Cholesky factorization to compute the solution, error-bound and condition estimate
	for a complex Hermitian positive-definite system of linear equations
F07GAF	Computes the solution to a real symmetric positive-definite system of linear equations, packed storage
F07GBF	Uses the Cholesky factorization to compute the solution, error-bound and condition estimate for a real symmetric positive-definite system of linear equations, packed storage
F07GNF	Computes the solution to a complex Hermitian positive-definite system of linear equations, packed storage
F07GPF	Uses the Cholesky factorization to compute the solution, error-bound and condition estimate for a complex Hermitian positive-definite system of linear equations, packed storage

F07HAF Computes the solution to a real symmetric positive-definite banded system of linear equations

F07HBF	Uses the Cholesky factorization to compute the solution, error-bound and condition estimate for a real symmetric positive-definite banded system of linear equations
F07HNF	Computes the solution to a complex Hermitian positive-definite banded system of linear equations
F07HPF	Uses the Cholesky factorization to compute the solution, error-bound and condition estimate for a complex Hermitian positive-definite banded system of linear equations
F07JBF	Uses the modified Cholesky factorization to compute the solution, error-bound and condition estimate for a real symmetric positive-definite tridiagonal system of linear equations
F07JPF	Uses the modified Cholesky factorization to compute the solution, error-bound and condition estimate for a complex Hermitian positive-definite tridiagonal system of linear equations
F07MBF	Uses the diagonal pivoting factorization to compute the solution to a real symmetric system of linear equations
F07MPF	Uses the diagonal pivoting factorization to compute the solution to a complex Hermitian system of linear equations
F07NPF	Uses the diagonal pivoting factorization to compute the solution to a complex symmetric system of linear equations
F07PBF	Uses the diagonal pivoting factorization to compute the solution to a real symmetric system of linear equations, packed storage
F07PPF	Uses the diagonal pivoting factorization to compute the solution to a complex Hermitian system of linear equations, packed storage
F07QPF	Uses the diagonal pivoting factorization to compute the solution to a complex symmetric system of linear equations, packed storage
F08AAF	Solves an overdetermined or underdetermined real linear system
F08ANF	Solves an overdetermined or underdetermined complex linear system
F08BAF	Computes the minimum-norm solution to a real linear least-squares problem
F08BFF	QR factorization of real general rectangular matrix with column pivoting, using BLAS-3
F08BNF	Computes the minimum-norm solution to a complex linear least-squares problem
F08BTF	QR factorization of complex general rectangular matrix with column pivoting, using BLAS-3
F08FAF	Computes all eigenvalues and, optionally, eigenvectors of a real symmetric matrix
F08FBF	Computes selected eigenvalues and, optionally, eigenvectors of a real symmetric matrix
F08FCF	All eigenvalues and optionally all eigenvectors of real symmetric matrix (divide-and-conquer)
F08FDF	Computes selected eigenvalues and, optionally, eigenvectors of a real symmetric matrix (Relatively Robust Representations)
F08FGF	Apply orthogonal transformation determined by F08FEF (DSYTRD)
F08FNF	Computes all eigenvalues and, optionally, eigenvectors of a complex Hermitian matrix
F08FPF	Computes selected eigenvalues and, optionally, eigenvectors of a complex Hermitian matrix
F08FQF	All eigenvalues and optionally all eigenvectors of complex Hermitian matrix (divide-and-conquer)
F08FRF	Computes selected eigenvalues and, optionally, eigenvectors of a complex Hermitian matrix (Relatively Robust Representations)
F08FUF	Apply unitary transformation matrix determined by F08FSF (ZHETRD)
F08GAF	Computes all eigenvalues and, optionally, eigenvectors of a real symmetric matrix, packed storage
F08GBF	Computes selected eigenvalues and, optionally, eigenvectors of a real symmetric matrix, packed storage
F08GCF	All eigenvalues and optionally all eigenvectors of real symmetric matrix, packed storage (divide-and-conquer)
F08GNF	Computes all eigenvalues and, optionally, eigenvectors of a complex Hermitian matrix, packed storage
F08GPF	Computes selected eigenvalues and, optionally, eigenvectors of a complex Hermitian matrix, packed storage
F08GQF	All eigenvalues and optionally all eigenvectors of complex Hermitian matrix, packed storage (divide-and-conquer)
F08HAF	Computes all eigenvalues and, optionally, eigenvectors of a real symmetric band matrix
F08HBF	Computes selected eigenvalues and, optionally, eigenvectors of a real symmetric band matrix
F08HCF	All eigenvalues and optionally all eigenvectors of real symmetric band matrix (divide-and-conquer)

F08HNF Computes all eigenvalues and, optionally, eigenvectors of a complex Hermitian band matrix

F08HPF	Computes selected eigenvalues and, optionally, eigenvectors of a complex Hermitian band matrix
F08HQF	All eigenvalues and optionally all eigenvectors of complex Hermitian band matrix (divide-and- conquer)
F08JAF	Computes all eigenvalues and, optionally, eigenvectors of a real symmetric tridiagonal matrix
F08JBF	Computes selected eigenvalues and, optionally, eigenvectors of a real symmetric tridiagonal matrix
F08JCF	All eigenvalues and optionally all eigenvectors of real symmetric tridiagonal matrix (divide- and-conquer)
F08JDF	Computes selected eigenvalues and, optionally, eigenvectors of a real symmetric tridiagonal matrix (Relatively Robust Representations)
F08JGF	All eigenvalues and eigenvectors of real symmetric positive-definite tridiagonal matrix, reduced from real symmetric positive-definite matrix
F08JHF	Computes all eigenvalues and, optionally, eigenvectors of a real symmetric tridiagonal matrix or a matrix reduced to this form (divide-and-conquer)
F08JLF	Computes all eigenvalues and, optionally, eigenvectors of a real symmetric tridiagonal matrix or a symmetric matrix reduced to this form (Relatively Robust Representations)
F08JUF	All eigenvalues and eigenvectors of real symmetric positive-definite tridiagonal matrix, reduced from complex Hermitian positive-definite matrix
F08JVF	Computes all eigenvalues and, optionally, eigenvectors of a real symmetric tridiagonal matrix or a complex Hermitian matrix reduced to this form (divide-and-conquer)
F08JYF	Computes all eigenvalues and, optionally, eigenvectors of a real symmetric tridiagonal matrix or a complex Hermitian matrix reduced to this form (Relatively Robust Representations)
F08KAF	Computes the minimum-norm solution to a real linear least-squares problem using singular value decomposition
F08KBF	Computes the singular value decomposition of a real matrix, optionally computing the left and/ or right singular vectors
F08KCF	Computes the minimum-norm solution to a real linear least-squares problem using singular value decomposition (divide-and-conquer)
F08KDF	Computes the singular value decomposition of a real matrix, optionally computing the left and/ or right singular vectors (divide-and-conquer)
F08KFF	Generate orthogonal transformation matrices from reduction to bidiagonal form determined by F08KEF (DGEBRD)
F08KGF	Apply orthogonal transformations from reduction to bidiagonal form determined by F08KEF (DGEBRD)
F08KNF	Computes the minimum-norm solution to a complex linear least-squares problem using singular value decomposition
F08KPF	Computes the singular value decomposition of a complex matrix, optionally computing the left and/or right singular vectors
F08KQF	Computes the minimum-norm solution to a complex linear least-squares problem using singular value decomposition (divide-and-conquer)
F08KRF	Computes the singular value decomposition of a complex matrix, optionally computing the left and/or right singular vectors (divide-and-conquer)
F08KTF	Generate unitary transformation matrices from reduction to bidiagonal form determined by F08KSF (ZGEBRD)
F08KUF	Apply unitary transformations from reduction to bidiagonal form determined by F08KSF (ZGEBRD)
F08MDF	Computes the singular value decomposition of a real bidiagonal matrix, optionally computing the singular vectors (divide-and-conquer)
F08NAF	Computes all eigenvalues and, optionally, left and/or right eigenvectors of a real nonsymmetric matrix
F08NBF	Computes all eigenvalues and, optionally, left and/or right eigenvectors of a real nonsymmetric matrix; also, optionally, the balancing transformation, the reciprocal condition numbers for the eigenvalues and for the right eigenvectors
F08NFF	Generate orthogonal transformation matrix from reduction to Hessenberg form determined by F08NEF (DGEHRD)
F08NGF	Apply orthogonal transformation matrix from reduction to Hessenberg form determined by F08NEF (DGEHRD)

F08NNF	Computes all eigenvalues and, optionally, left and/or right eigenvectors of a complex nonsymmetric matrix
F08NPF	Computes all eigenvalues and, optionally, left and/or right eigenvectors of a complex nonsymmetric matrix; also, optionally, the balancing transformation, the reciprocal condition numbers for the eigenvalues and for the right eigenvectors
F08NTF	Generate unitary transformation matrix from reduction to Hessenberg form determined by F08NSF (ZGEHRD)
F08NUF	Apply unitary transformation matrix from reduction to Hessenberg form determined by F08NSF (ZGEHRD)
F08PAF	Computes for real square nonsymmetric matrix, the eigenvalues, the real Schur form, and, optionally, the matrix of Schur vectors
F08PBF	Computes for real square nonsymmetric matrix, the eigenvalues, the real Schur form, and, optionally, the matrix of Schur vectors; also, optionally, computes reciprocal condition numbers for selected eigenvalues
F08PNF	Computes for complex square nonsymmetric matrix, the eigenvalues, the Schur form, and, optionally, the matrix of Schur vectors
F08PPF	Computes for real square nonsymmetric matrix, the eigenvalues, the Schur form, and, optionally, the matrix of Schur vectors; also, optionally, computes reciprocal condition numbers for selected eigenvalues
F08SAF	Computes all the eigenvalues, and optionally, the eigenvectors of a real generalized symmetric- definite eigenproblem
F08SBF	Computes selected eigenvalues, and optionally, the eigenvectors of a real generalized symmetric-definite eigenproblem
F08SCF	Computes all the eigenvalues, and optionally, the eigenvectors of a real generalized symmetric- definite eigenproblem (divide-and-conquer)
F08SNF	Computes all the eigenvalues, and optionally, the eigenvectors of a complex generalized Hermitian-definite eigenproblem
F08SPF	Computes selected eigenvalues, and optionally, the eigenvectors of a complex generalized Hermitian-definite eigenproblem
F08SQF	Computes all the eigenvalues, and optionally, the eigenvectors of a complex generalized Hermitian-definite eigenproblem (divide-and-conquer)
F08UAF	Computes all the eigenvalues, and optionally, the eigenvectors of a real banded generalized symmetric-definite eigenproblem
F08UBF	Computes selected eigenvalues, and optionally, the eigenvectors of a real banded generalized symmetric-definite eigenproblem
F08UCF	Computes all the eigenvalues, and optionally, the eigenvectors of a real banded generalized symmetric-definite eigenproblem (divide-and-conquer)
F08UNF	Computes all the eigenvalues, and optionally, the eigenvectors of a complex banded generalized Hermitian-definite eigenproblem
F08UPF	Computes selected eigenvalues, and optionally, the eigenvectors of a complex banded generalized Hermitian-definite eigenproblem
F08UQF	Computes all the eigenvalues, and optionally, the eigenvectors of a complex banded generalized Hermitian-definite eigenproblem (divide-and-conquer)
F08WAF	Computes, for a real nonsymmetric matrix pair, the generalized eigenvalues, and optionally, the left and/or right generalized eigenvectors
F08WBF	Computes, for a real nonsymmetric matrix pair, the generalized eigenvalues, and optionally, the left and/or right generalized eigenvectors; also, optionally, the balancing transformation, the reciprocal condition numbers for the eigenvalues and for the right eigenvectors
F08WNF	Computes, for a complex nonsymmetric matrix pair, the generalized eigenvalues, and optionally, the left and/or right generalized eigenvectors
F08WPF	Computes, for a complex nonsymmetric matrix pair, the generalized eigenvalues, and optionally, the left and/or right generalized eigenvectors; also, optionally, the balancing transformation, the reciprocal condition numbers for the eigenvalues and for the right
F08XAF	eigenvectors Computes, for a real nonsymmetric matrix pair, the generalized eigenvalues, the generalized
F08XBF	real Schur form and, optionally, the left and/or right matrices of Schur vectors Computes, for a real nonsymmetric matrix pair, the generalized eigenvalues, the generalized real Schur form and, optionally, the left and/or right matrices of Schur vectors; also, optionally, computes reciprocal condition numbers for selected eigenvalues

F08XNF	Computes, for a complex nonsymmetric matrix pair, the generalized eigenvalues, the
	generalized complex Schur form and, optionally, the left and/or right matrices of Schur vectors
F08XPF	Computes, for a complex nonsymmetric matrix pair, the generalized eigenvalues, the
	generalized complex Schur form and, optionally, the left and/or right matrices of Schur
	vectors; also, optionally, computes reciprocal condition numbers for selected eigenvalues
F08ZAF	Solves the real linear equality-constrained least-squares (LSE) problem
F08ZBF	Solves a real general Gauss-Markov linear model (GLM) problem
F08ZEF	Computes a generalized $QR$ factorization of a real matrix pair
F08ZFF	Computes a generalized $RQ$ factorization of a real matrix pair Solves the complex linear equality constrained losst equation (LSE) methods
F08ZNF	Solves the complex linear equality-constrained least-squares (LSE) problem
F08ZPF	Solves a complex general Gauss-Markov linear model (GLM) problem
F08ZSF	Computes a generalized $QR$ factorization of a complex matrix pair
F08ZTF	Computes a generalized $RQ$ factorization of a complex matrix pair Solution of real groups required in our production $RCMPES$ and $RC$
F11DCF	Solution of real sparse nonsymmetric linear system, RGMRES, CGS, Bi-CGSTAB or TFQMR method, preconditioner computed by F11DAF
F11DEF	Solution of real sparse nonsymmetric linear system, RGMRES, CGS, Bi-CGSTAB, or
	TFQMR method, Jacobi or SSOR preconditioner (Black Box)
F11DKF	Real sparse nonsymmetric linear systems, line Jacobi preconditioner
F11DQF	Solution of complex sparse non-Hermitian linear system, RGMRES, CGS, Bi-CGSTAB or
	TFQMR method, preconditioner computed by F11DNF (Black Box)
F11DSF	Solution of complex sparse non-Hermitian linear system, RGMRES, CGS, Bi-CGSTAB or
	TFQMR method, Jacobi or SSOR preconditioner Black Box
F11DXF	Complex sparse nonsymmetric linear systems, line Jacobi preconditioner
F11JCF	Solution of real sparse symmetric linear system, conjugate gradient/Lanczos method,
	preconditioner computed by F11JAF (Black Box)
F11JEF	Solution of real sparse symmetric linear system, conjugate gradient/Lanczos method, Jacobi or
	SSOR preconditioner (Black Box)
F11JQF	Solution of complex sparse Hermitian linear system, conjugate gradient/Lanczos method,
	preconditioner computed by F11JNF (Black Box)
F11JSF	Solution of complex sparse Hermitian linear system, conjugate gradient/Lanczos method,
	Jacobi or SSOR preconditioner (Black Box)
F12FCF	Returns the converged approximations (as determined by F12ABF) to eigenvalues of a real
	symmetric sparse (standard or generalized) eigenproblem and, optionally, the corresponding
	approximate eigenvectors and/or an orthonormal basis for the associated approximate invariant
	subspace
F12FGF	Computes approximations to selected eigenvalues of a real symmetric banded (standard or
	generalized) eigenproblem and, optionally, the corresponding approximate eigenvectors and/or
	an orthonormal basis for the associated approximate invariant subspace
G01HBF	Computes probabilities for the multivariate Normal distribution
G02BYF	Computes partial correlation/variance-covariance matrix from correlation/variance-covariance
~ ~ ~ ~ ~ ~	matrix computed by G02BXF
G02CGF	Multiple linear regression, from correlation coefficients, with constant term
G02CHF	Multiple linear regression, from correlation-like coefficients, without constant term
G02DAF	Fits a general (multiple) linear regression model
G02DDF	Estimates of linear parameters and general linear regression model from updated model
G02DEF	Add a new independent variable to a general linear regression model
G02DGF	Fits a general linear regression model to new dependent variable
G02DKF	Estimates and standard errors of parameters of a general linear regression model for given
CODEAE	constraints
G02EAF	Computes residual sums of squares for all possible linear regressions for a set of independent
CONFEE	variables
G02EEF	Fits a linear regression model by forward selection
G02GAF	Fits a generalized linear model with Normal errors
G02GBF	Fits a generalized linear model with Boisson arrors
G02GCF	Fits a generalized linear model with Poisson errors
G02GDF G02GKF	Fits a generalized linear model with gamma errors Estimates and standard errors of parameters of a general linear model for given constraints
G02GKF G02HAF	Estimates and standard errors of parameters of a general linear model for given constraints Robust regression, standard <i>M</i> -estimates
G02HAF G02HDF	Robust regression, standard <i>M</i> -estimates Robust regression, compute regression with user-supplied functions and weights
0021101	Robust regression, compute regression with user-supplied functions and weights

G02HFF Robust regression, variance-covariance matrix following G02HDF G02JAF Linear mixed effects regression using Restricted Maximum Likelihood (REML) G03AAF Performs principal component analysis G03ACF Performs canonical variate analysis G03ADF Performs canonical correlation analysis Computes orthogonal rotations for loading matrix, generalized orthomax criterion G03BAF G03BCF **Computes Procrustes rotations** G03CAF Computes maximum likelihood estimates of the parameters of a factor analysis model, factor loadings, communalities and residual correlations Computes test statistic for equality of within-group covariance matrices and matrices for G03DAF discriminant analysis G03FAF Performs principal co-ordinate analysis, classical metric scaling Analysis of variance, randomized block or completely randomized design, treatment means G04BBF and standard errors G04BCF Analysis of variance, general row and column design, treatment means and standard errors G05PCF Generates a realisation of a multivariate time series from a VARMA model G08RAF Regression using ranks, uncensored data G08RBF Regression using ranks, right-censored data G11CAF Returns parameter estimates for the conditional analysis of stratified data Contingency table, latent variable model for binary data G11SAF G12BAF Fits Cox's proportional hazard model G13ADF Univariate time series, preliminary estimation, seasonal ARIMA model G13AEF Univariate time series, estimation, seasonal ARIMA model (comprehensive) Univariate time series, estimation, seasonal ARIMA model (easy-to-use) G13AFF G13AJF Univariate time series, state set and forecasts, from fully specified seasonal ARIMA model G13ASF Univariate time series, diagnostic checking of residuals, following G13AEF or G13AFF G13BAF Multivariate time series, filtering (pre-whitening) by an ARIMA model G13BBF Multivariate time series, filtering by a transfer function model G13BDF Multivariate time series, preliminary estimation of transfer function model Multivariate time series, estimation of multi-input model G13BEF Multivariate time series, state set and forecasts from fully specified multi-input model G13BJF G13DBF Multivariate time series, multiple squared partial autocorrelations Multivariate time series, estimation of VARMA model G13DCF Multivariate time series, forecasts and their standard errors G13DJF G13DNF Multivariate time series, sample partial lag correlation matrices,  $\chi^2$  statistics and significance levels G13DPF Multivariate time series, partial autoregression matrices G13DSF Multivariate time series, diagnostic checking of residuals, following G13DCF G13DXF Calculates the zeros of a vector autoregressive (or moving average) operator G13EBF Combined measurement and time update, one iteration of Kalman filter, time-invariant, square root covariance filter G13FAF Univariate time series, parameter estimation for either a symmetric GARCH process or a GARCH process with asymmetry of the form  $(\epsilon_{t-1} + \gamma)^2$ Univariate time series, parameter estimation for a GARCH process with asymmetry of the G13FCF form  $(|\epsilon_{t-1}| + \gamma \epsilon_{t-1})^2$ Univariate time series, parameter estimation for an asymmetric Glosten, Jagannathan and G13FEF Runkle (GJR) GARCH process

G13FGF Univariate time series, parameter estimation for an exponential GARCH (EGARCH) process